Mesh and Nodal Analysis

Here, two very powerful analysis methods will be introduced for analysing any circuit:

- 1. Node analysis (Node-voltage method)
- 2. Mesh analysis (Mesh-current method)

These methods are based on the systematic application of Kirchhoff's laws (KVL and KCL).

Nodal Analysis

- Six steps:
 - 1. Chose one node as the reference node
 - 2. Label remaining nodes V_1 , V_2 , etc.
 - 3. Label any known voltages
 - 4. Apply Kirchhoff's current law to each unknown node
 - 5. Solve simultaneous equations to determine voltages
 - 6. If necessary calculate required currents







Solution: (continued)

- solving these two equations gives

$$V_2 = 32.34$$
 V
 $V_3 = 40.14$ V

- and the required current is given by

$$I_1 = \frac{V_3}{25\,\Omega} = \frac{40.14\,\text{V}}{25\,\Omega} = 1.6\,\text{A}$$







Mesh Analysis

• Four steps:

- 1. Identify the meshes and assign a clockwise-flowing current to each. Label these I_1, I_2 , etc.
- 2. Apply Kirchhoff's voltage law to each mesh
- 3. Solve the simultaneous equations to determine the currents I_1, I_2 , etc.
- 4. Use these values to obtain voltages if required







Solution: (continued)

 $-\,$ the voltage across the 10 Ω resistor is therefore given by

 $V_{\varepsilon} = R_{\varepsilon}(I_3 - I_2)$ = 10(0.053 - 0.034) = 0.19 V

 since the calculated voltage is positive, the polarity is as shown on the figure with the left hand end of the resistor more positive than the right hand end

Solving Simultaneous Circuit Equations

- Both nodal analysis and mesh analysis produce a series of simultaneous equations
 - $-\,$ can be solved 'by hand' or by using matrix methods

– e.g.

 $\begin{array}{l} 50-160l_{_1}+20l_{_2}+30l_{_3}=0\\ 20l_{_1}-210l_{_2}+10l_{_3}=0\\ 30l_{_1}+10l_{_2}-190l_{_3}=0 \end{array}$

- can be rearranged as

 $\begin{array}{l} 160l_{1}^{\prime}-20l_{2}^{\prime}-30l_{3}^{\prime}=50\\ 20l_{1}^{\prime}-210l_{2}^{\prime}+10l_{3}^{\prime}=0\\ 30l_{1}^{\prime}+10l_{2}^{\prime}-190l_{3}^{\prime}=0 \end{array}$

Solving Simultaneous Circuit Equations

- these equations can be expressed as

60	-20	-30	I,		50
20	-210	10	I_2	=	0
30	10	-190	I_3		C

- which can be solved by hand (e.g. Cramer's rule)
- or can use automated tools
 - e.g. scientific calculators
 - computer-based packages such as MATLAB or Mathcad







